

Health economic evaluation: a very Bayesian thing

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That's us (or is it?)...





Nixon

Jackson

Baio



- Health economic evaluation
 - What is health economics?
 - What does health economics do?



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 - Models for individual-level data
 - Models for aggregated data



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 - Cost-effectiveness/cost-utility analysis
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- Uncertainty analysis
 - Rationale
 - Main ideas



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 - Rationale
 - Main ideas
- Conclusions

What is health economics?



What is health economics?

		-		
Cardiovascular system (C)	Expenditure ¹	%	DDD ²	%*
Bosentan	37.0	47.9	0.3	0.2
Cardiac stimulants	8.8	11.4	3.5	2.1
Statins	5.5	7.2	15.9	9.9
Calcium Antagonists (diidro.)	4.5	5.8	20.1	12.4
litrates	3.7	4.8	21.0	13.0
Diuretics	2.2	2.8	18.8	11.6
Ace Inhibitors	2.1	2.8	24.0	14.8
Beta Blockers	1.7	2.2	17.2	10.7
Alfa Blockers	1.0	1.3	3.2	2.0
Angiotensin II Antagonists	0.9	1.1	3.5	2.2

¹ Millions €

² Millions days of therapy

'Percentages are calculated over the total of the ATC category

Source: Osmed (2007)



Budgeting



What is health economics?



Generalisation and integration of statistics (methodological & experimental), epidemiology, econometrics and financial analysis

What does health economics do?

- **Objective**: Combine costs & benefits of a given intervention into a rational scheme for allocating resources
 - Recently, models have been built upon more advanced statistical foundations
 - This problem can be formalised within a statistical decision-theoretic approach. Rational decision-making is effected through the comparison of expected utilities
 - Incremental approach: need to consider at least two interventions

- **Objective**: Combine costs & benefits of a given intervention into a rational scheme for allocating resources
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 - This problem can be formalised within a statistical decision-theoretic approach. Rational decision-making is effected through the comparison of expected utilities
 - Incremental approach: need to consider at least two interventions
- Increasingly under a **Bayesian framework**, especially in the UK: 5.9.10–12 Dealing with parameter uncertainty in cost-effectiveness analysis (NICE Methods for Technology Assessment)
 - All inputs used in the analysis will be estimated with a degree of imprecision.
 - Probabilistic sensitivity analysis is preferred for translating the imprecision in all input variables into a measure of decision uncertainty in the cost-effectiveness of the options being compared.
 - Appropriate ways of presenting uncertainty include confidence ellipses and scatter plots on the cost-effectiveness plane (when the comparison is restricted to two alternatives) and cost-effectiveness acceptability curves.

Health economic outcome

- One of the most important characteristic of health economic data is that we have **multivariate outcomes**
 - e = suitable measure of clinical benefit of an intervention
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- We typically need to assess these quantities jointly
 - Costs and benefit will tend to be correlated
 - Strong positive correlation effective treatments are innovative and result from intensive and lengthy research ⇒ are associated with higher unit costs
 - Negative correlation more effective treatments may reduce total care pathway costs e.g. by reducing hospitalisations, side effects, etc.
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- There are different ways in which we can define (e, c) for a specific problem
 - Direct vs indirect vs intangible costs
 - "Hard-" vs utility-based clinical outcomes
 - Public (e.g. NHS) vs private (e.g. insurance) perspective





- Estimates relevant population parameters
- Varies with the type of available data (& statistical approach!)



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- average measure for costs and clinical benefits
 Varies with the type of
- Varies with the type of available data & statistical model used

Health economic evaluations



Health economic evaluations





- Estimates relevant population parameters
- Varies with the type of available data (& statistical approach!)

- Combines the parameters to obtain a population average measure for costs and clinical benefits
- Varies with the type of available data & statistical model used

- Summarises the economic model by computing suitable measures of "cost-effectiveness"
- Dictates the best course of actions, given current evidence
- Standardised process

1. Statistical modelling



- Sampling variability for the health economic outcomes is described by a distribution p(e, c | θ^t), which depends on a set of population parameters θ^t
 - Probability of some clinical outcome
 - Duration in treatment
 - Reduction in the rate of occurrence of some event
 - Unit cost of acquisition of a health technology



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- The way in which we construct our statistical model, depends on
 - The characteristic of the available data (individual-level vs aggregated data)
 - The statistical framework (Bayesian vs frequentist)

RCTs vs decision-analytical models

- RCTs are a key component in the evaluation of health care interventions
 - Usually individual-level data are collected for a clinical study and increasingly often complemented by financial outcomes
- However, there may issues with RCTs data
 - Comparator(s) in the trial may not reflect standard of care
 - Limited follow up
 - Small sample size
 - Poor external validity

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 - Poor external validity
- Health economic evaluations should include information from as many sources as possible
 - Evidence synthesis of literature
 - Network meta-analysis
- Bayesian methods ideally placed to deal with these!

- Observe a vector (e_i,c_i) under each intervention being compared
 - May also observe other variables (covariates) *e.g.* individual values for age, sex, co-morbidities, etc
- Use observed data to estimate the relevant population parameters $\pmb{\theta}^t = (\pmb{\theta}_e^t, \pmb{\theta}_c^t)$
 - These are generally vectors, made by several components (*e.g.* means, variances, rates, etc)
- The main interest is in the population average benefits and costs under treatment \boldsymbol{t}

 $\mu_e^t = \mathsf{E}[e \mid \pmb{\theta}^t] \qquad \text{and} \qquad \mu_c^t = \mathsf{E}[c \mid \pmb{\theta}^t]$

- NB: Because of underlying correlation, it is necessary to use some form of joint model
 - But: simple models (such as bivariate Normal) are not suitable, as both e,c tend to be skewed and cost are positive

Can factorise the joint distribution, for example as $p(e, c) = p(c)p(e \mid c)$



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For instance, can model

- $c_{it} \sim \text{Gamma}(\eta_t, \lambda_t)$ [rate & shape] $\Rightarrow \mu_{ct} = \eta_t / \lambda_t$
 - $c_{it} \sim \log \operatorname{Normal}(\eta_t, \lambda_t) \ [\log \text{ mean \& log sd}] \Rightarrow \mu_{ct} = \exp\left(\eta_t + \lambda_t^2/2\right)$

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• $\mathsf{E}[e_{it}] = \phi_{it}; \ g(\phi_{it}) = \xi_t + \gamma_t(c_{it} - \mu_{ct}) \Rightarrow \mu_{et} = g^{-1}(\xi_t)$

Decision-analytic models



- These can in turn be used to construct a "population model" to describe the disease history and its implications
 - Decision trees
 - Markov (multistate) models

Decision-analytic models

- Often, we do not have access to individual data and all we have is a set of aggregated data on relevant quantities
- These can in turn be used to construct a "population model" to describe the disease history and its implications

- Decision trees
- Markov (multistate) models





- Data sources for a decision-analytic model include
 - Published literature (e.g. probability of influenza in the range [0.2 0.4])
 - Evidence synthesis/meta-analysis
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 - Published literature (e.g. probability of influenza in the range [0.2 0.4])
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 - Expert opinions
- We need to combine the parameters of the population model to derive suitable measures of costs and benefits

$$-c_0 = (1 - p_t)c^{\text{GP}} + p_t \left(c^{\text{GP}} + c^{\text{Inf}}\right) \Rightarrow \text{avg cost for } t = 0$$

$$-c_1 = (1 - p_t) \left(c^{\text{GP}} + c^{\text{NI}} \right) + p_t \left(c^{\text{GP}} + c^{\text{NI}} + c^{\text{Inf}} \right) \Rightarrow \text{avg cost for } t = 1$$

- $e_t = lp_t \Rightarrow$ avg measure of clinical benefit
- **NB**: Again, under the Bayesian framework, all the parameters are modelled and the uncertainty is fully accounted for!

Decision-analytic models





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Health Economics: a very Bayesian thing

- Cost minimisation
 - Assumes that the benefits produced by two interventions are identical \Rightarrow the only dimension of interest is costs
- Cost-benefit analysis
 - Requires that costs and benefits are converted and analysed into monetary terms \Rightarrow difficulties in valuing health outcomes in monetary units

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• Cost-effectiveness analysis (CEA)

- Evaluates cost-per-outcome gained
- Outcomes are usually "hard" measurements (eg death) ⇒ easy to understand for clinicians, but difficult to compare across diseases (may have different main outcome)

• Cost-utility analysis (CUA)

- Considers a common health outcome unit (= QALYs), so easy to compare across diseases
- Often interchangeable with CEA (common methodology!)

2. Economic modelling

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Can think of this step as the process of obtaining relevant population summaries for the measures of cost & clinical benefits. For example, when comparing two interventions t = 0, 1, the main focus is on

• The increment in mean benefits

$$\Delta_e = \underbrace{\mathsf{E}[e \mid \theta^1]}_{\mu_1^e} - \underbrace{\mathsf{E}[e \mid \theta^0]}_{\mu_0^e}$$

• The increment in mean costs:

$$\Delta_c = \underbrace{\mathsf{E}[c \mid \theta^1]}_{\mu_1^c} - \underbrace{\mathsf{E}[c \mid \theta^0]}_{\mu_0^c}$$

- **NB**: In a Bayesian context, these are functions of θ and thus random variables!
- Also, when using individual-level data, estimation typically directly available from the statistical model

3. (Bayesian) Decision analysis

Based on the precepts of expected utility theory

- **1** Characterise variability in the observable outcomes and uncertainty in the parameters using a model $p(e, c, \theta^t) = p(e, c \mid \theta^t)p(\theta^t)$
- 2 Value the consequences of decisions through the future outcomes, using a suitable utility function u(e,c;t)
 - Typically choose the monetary net benefit u(e,c;t) := ke c
 - k = "willingness to pay" = cost per extra unit of effectiveness gained
- **3** For each intervention t, compute the expected utility $U^t = \mathsf{E}[u(e,c;t)]$
- 4 Choose the intervention that maximises the expected utility
 - It is possible to prove that this is equivalent to maximising the chance of obtaining the preferred outcome

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 $\ensuremath{\textbf{NB}}\xspace$: When only two interventions are being compared, this is equivalent to assessing whether

$$\mathsf{EIB} = \mathcal{U}^1 - \mathcal{U}^0 > 0$$

So, if EIB > 0 then t = 1 is more cost-effective than t = 0

EIB vs ICER



• Alternative criterion for making decisions

 $\mathsf{ICER} = \frac{\mathsf{E}[\Delta_c]}{\mathsf{E}[\Delta_e]} = \mathsf{Additional\ cost\ to\ gain\ 1\ unit\ of\ benefit}$

$$\begin{split} - & \Delta_e = \underbrace{\mathsf{E}[e \mid \theta^1]}_{\mu_1^e} - \underbrace{\mathsf{E}[e \mid \theta^0]}_{\mu_0^e} = \text{increment in mean benefits} \\ - & \Delta_c = \underbrace{\mathsf{E}[c \mid \theta^1]}_{\mu_1^e} - \underbrace{\mathsf{E}[c \mid \theta^0]}_{\mu_0^e} = \text{increment in mean costs} \end{split}$$

• When the MNB is used as utility function and $\mathcal{T}=(0,1)$

$$\mathsf{EIB} = \mathcal{U}^1 - \mathcal{U}^0 = \mathsf{E}[k\Delta_e - \Delta_c] = k\mathsf{E}[\Delta_e] - \mathsf{E}[\Delta_c]$$

and thus

$$\mathsf{EIB} > 0 \Rightarrow k > \frac{\mathsf{E}[\Delta_c]}{\mathsf{E}[\Delta_e]} = \mathsf{ICER}$$

Cost-effectiveness plane vs ICER



Cost-effectiveness plane

Effectiveness differential

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Cost differential

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Cost-effectiveness plane vs ICER



Cost differential

Effectiveness differential

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EIB vs ICER

• Another criterion for making decisions is based on

$$ICER = \frac{E[\Delta_c]}{E[\Delta_e]} = Additional \text{ cost to gain 1 unit of benefit}$$

- $\Delta_e = \underbrace{\mathsf{E}[e \mid \theta^1]}_{\mu_1^e} \underbrace{\mathsf{E}[e \mid \theta^0]}_{\mu_0^e} = \text{increment in mean benefits}$ • $\Delta_c = \underbrace{\mathsf{E}[c \mid \theta^1]}_{\mu_1^c} - \underbrace{\mathsf{E}[c \mid \theta^0]}_{\mu_0^e} = \text{increment in mean costs}$
- When the MNB is used as utility function and $\mathcal{T} = (0,1)$

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Cost-effectiveness plane vs EIB vs ICER





Effectiveness differential

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Cost-effectiveness plane vs EIB vs ICER





Effectiveness differential

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Health economic evaluation based on EIB



Expected Incremental Benefit

So: problem solved?





So: problem solved?... Well, not really!



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- The quality of the current evidence is often limited
 - During the pre-market authorisation phase, the regulator should decide whether to grant reimbursement to a new product — and in some countries also set the price — on the basis of uncertain evidence, regarding both clinical and economic outcomes
 - Although it is possible to answer some unresolved questions after market authorisation, relevant decisions such as that on reimbursement (which determines the overall access to the new treatment) have already been taken



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- This leads to the necessity of performing (*probabilistic*) sensitivity analysis (**PSA**)
 - Formal quantification of the impact of uncertainty in the parameters on the results of the economic model
 - Standard requirement in many health systems (e.g. for NICE in the UK), but still not universally applied
 - Often limited to *parametric* uncertainty, but should be extended to *structural* uncertainty too (more on these in the next talks!)

Parameters

Model structure Old chemotherapy





Parameters

Model structure Old chemotherapy





Parameters

Model structure Old chemotherapy





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Parameters

Model structure Old chemotherapy





Old chemotherapy		
Benefits	Costs	
741	670 382.1	
699	871273.3	
726	425 822.2	
743.1	656 644.6	

New chemotherapy				
Benefits	Costs			
732	1 131 978			
664	1 325 654			
811	766 411.4			
794.6	991 804.0			



Conclusions

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 - Previous studies
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- In general, Bayesian models are more flexible and allow the inclusion of complex relationships between variables and parameters
 - This is particularly effective in decision-models, where information from different sources may be combined into a single framework
 - Useful in the case of individual-level data (eg from Phase III RCT)

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 - This is particularly effective in decision-models, where information from different sources may be combined into a single framework
 - Useful in the case of individual-level data (eg from Phase III RCT)
- Using MCMC methods, it is possible to produce the results in terms of simulations from the posterior distributions
 - These can be used to build suitable variables of cost and benefit
 - Particularly effective for running "probabilistic sensitivity analysis"



Thank you!